## Work, energy and power 2D

- 1 Power = Fv=  $1500 \times 12$ = 18000
- The power is 18 kW
- 2 Power = Fv=  $1000 \times 15$ = 15000The power is 15 000 W (or 15 kW)
- 3 Power = Fv  $5000 = F \times 18$   $F = \frac{5000}{18}$ = 277.7...

The driving force has magnitude 278 N (3 s.f.)

4  $\longrightarrow$  0 m s<sup>-2</sup> At maximum speed the acceleration is zero.

Resolving horizontally: T = 600Power = Fv15000 = 600v15000

$$v = \frac{15000}{600}$$
$$= 25$$

The maximum speed is 25 m s<sup>-1</sup>

5 a  $\longrightarrow$  40 m s<sup>-1</sup>  $\longrightarrow$  0 m s<sup>-2</sup> At maximum speed the acceleration is zero.

Resolving horizontally: T = 500Power = Fv=  $500 \times 40$ = 20000

The power is 20 000 W (or 20 kW)

**b** The resistance to motion of the car would typically be expected to increase with speed but it would be reasonable to assume a constant resistive force if the car maintained the same speed and the gradient and surface of the road stayed the same.

6 
$$\longrightarrow$$
 16 m s<sup>-1</sup>  $\longrightarrow$  0 m s<sup>-2</sup>



Power = 
$$Fv$$

$$8.8 \times 10^3 = T \times 16$$

$$T = \frac{8800}{16}$$

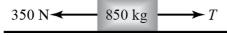
$$T = 550$$

Resolving horizontally: R = T

$$R = 550$$

The magnitude of the resistance is 550 N

## 7 a $\longrightarrow$ 7 m s<sup>-1</sup> $\longrightarrow$ a m s<sup>-2</sup>



Power = 
$$Fv$$

$$9000 = T \times 7$$

$$T = \frac{9000}{7}$$

Now using F = ma:

$$T - 350 = ma$$

$$\frac{9000}{7}$$
 - 350 = 850a

$$a = \frac{9000}{7} - 350$$

$$a = 1.100...$$

The acceleration is  $1.10 \text{ m s}^{-2}$  (3 s.f.)

**b**  $\longrightarrow$  15 m s<sup>-1</sup>  $\longrightarrow$  a m s<sup>-2</sup>



Power = 
$$Fv$$

$$9000 = T \times 15$$

$$T = \frac{900}{15} = 600$$

Now using F = ma:

$$T - 350 = ma$$

$$600 - 350 = 850a$$

$$a = \frac{250}{850}$$

$$a = 0.2941...$$

The acceleration is  $0.294 \text{ m s}^{-2}$  (3 s.f.)

First find the tractive force produced by the engine and then

use F = ma to find the acceleration.

 $\longrightarrow$   $v \text{ m s}^{-1}$ 

7 c

Resolving horizontally: T = 350

Power = 
$$Fv$$

$$9000 = 350v$$

$$v = \frac{9000}{350}$$

$$v = 25.71...$$

The maximum speed is 25.7 m  $s^{-1}$  (3 s.f.)

8

$$\longrightarrow$$
 20 m s<sup>-1</sup>  $\longrightarrow$  0.3 m s<sup>-2</sup>

$$300 \text{ N} \longleftrightarrow 900 \text{ kg} \longrightarrow T$$

Using F = ma:

$$T - 300 = 900 \times 0.3$$

$$T = 900 \times 0.3 + 300$$

$$=570$$

Power = 
$$Fv$$

$$=570\times20$$

$$=11400$$

The power development by the engine is 11 400 W (or 11.4 kW)

9

$$\longrightarrow$$
 24 m s<sup>-1</sup>  $\longrightarrow$  0.2 m s<sup>-2</sup>

$$R \longleftarrow 1000 \text{ kg} \longrightarrow T$$

Power = 
$$Fv$$

$$12\ 000 = T \times 24$$

$$T = \frac{12\ 000}{24} = 500$$

Using F = ma:

$$T - R = 1000 \times 0.2$$

$$500 - R = 200$$

$$R = 500 - 200$$

$$R = 300$$

The value of R is 300.

4

10

 $\longrightarrow$   $\nu$  m s<sup>-1</sup>  $\longrightarrow$  0 m s<sup>-2</sup>

$$28 \text{ N} \longleftrightarrow T$$

Resolving horizontally:

$$T = 28$$

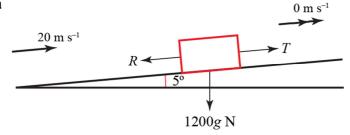
Power = Fv

$$280 = 28v$$

$$v = 10$$

The cyclist's maximum speed is 10 m s<sup>-1</sup>

11 a



Power = 
$$Fv$$

$$24\,000 = T \times 20$$

$$T = \frac{24\,000}{20} = 1200$$

Resolving parallel to the slope:

$$T = R + 1200g \sin 5^{\circ}$$

$$1200 = R + 1200g \sin 5^{\circ}$$

$$R = 1200 - 1200g \sin 5^{\circ}$$

$$R = 175.04...$$

The value of R is 175 (3 s.f.)

b

$$\longrightarrow$$
 20 m s<sup>-1</sup>  $\longrightarrow$  a m s<sup>-2</sup>

$$175 \text{ N} \longleftrightarrow 1200 \text{ kg} \longrightarrow T$$

From part **a**, T = 1200 N

Using 
$$F = ma$$
:

$$1200 - 175 = 1200a$$

$$a = \frac{1200 - 175}{1200}$$

$$a = 0.8541...$$

The initial acceleration of the van is  $0.854 \text{ m s}^{-2} (3 \text{ s.f.})$ 

12 a

$$750 \text{ N} \longleftrightarrow 800 \text{ kg} \longrightarrow T$$

 $\longrightarrow$  18 m s<sup>-1</sup>  $\longrightarrow$  a m s<sup>-2</sup>

Power = 
$$Fv$$

$$26000 = T \times 18$$

$$T = \frac{26000}{18}$$

Using F = ma:

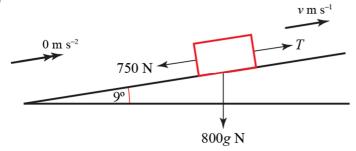
$$T - 750 = 800a$$

$$800a = \frac{26000}{18} - 750$$

$$a = 0.8680...$$

a = 0.8680...The acceleration is 0.868 m s<sup>-2</sup> (3 s.f.)

b



Resolving parallel to the slope:

$$T = 750 + 800g \sin 9^{\circ}$$

Power = 
$$Fv$$

$$26000 = T \times v$$

$$26000 = (750 + 800 \times 9.8 \sin 9^{\circ})v$$

$$v = \frac{26000}{(750 + 800 \times 9.8 \sin 9^\circ)}$$

$$v = 13.15...$$

The maximum speed is 13.2 m s<sup>-1</sup> (3 s.f.)

$$\longrightarrow$$
 0 m s<sup>-2</sup>  $\longrightarrow$  30 m s<sup>-1</sup>

$$600 \text{ N} \longleftrightarrow 1500 \text{ kg} \longrightarrow T$$

Resolving horizontally: T = 600

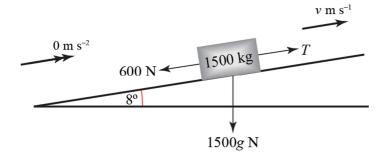
Power = 
$$Fv$$

$$=600 \times 30$$

$$=18000$$

The power is 18 000 W (or 18 kW)

## b



Resolving parallel to the slope:

$$T = 600 + 1500g\sin 8^{\circ}$$

Power = 
$$Fv$$

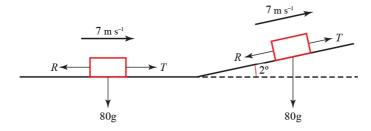
$$18000 = (600 + 1500g \sin 8^{\circ})v$$

$$v = \frac{18000}{(600 + 1500g\sin 8^\circ)}$$

$$=6.803...$$

The maximum speed is  $6.80 \text{ m s}^{-1} (3 \text{ s.f.})$ 

14



Consider the cyclist on level ground:

Power = Tv

Power = 7T

Since the velocity is constant, resolving horizontally:

T = R

So power = 7R

Consider the cyclist cycling uphill:

Power = Tv

Power = 7T

Since the velocity is constant, resolving parallel to the plane:

 $T = R + 80g \sin 2^{\circ}$ 

So power =  $7T = 7(R + 80g \sin 2^\circ) = 7R + 560g \sin 2^\circ$ 

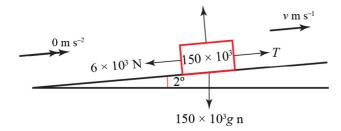
Therefore, the increase in power required is:

 $(7R + 560g \sin 2^{\circ}) - 7R = 560g \sin 2^{\circ}$ 

=191.5...

The increase in power required is 192 W (3 s.f.)

15 a



Resolving parallel to the slope:

$$T = (6 \times 10^3) + (150 \times 10^3 g \sin 2^\circ)$$

Power = Fv

$$350 \times 10^3 = (6 \times 10^3 + 150 \times 10^3 g \sin 2^\circ) \times v$$

$$v = \frac{350}{(6+150\times9.8\sin 2^\circ)}$$
  
= 6.107...

The maximum speed is 6.11 m s<sup>-1</sup>

1 tonne =  $10^3$  kg. When tonnes, kilonewtons and kilowatts are used the  $10^3$  will cancel, leaving easier numbers.

b

$$\longrightarrow$$
 6.107 m s<sup>-1</sup>  $\longrightarrow$  a m s<sup>-2</sup>

$$6 \times 10^3 \text{ N} \longleftarrow 150 \times 10^3 \text{ kg} \longrightarrow T$$

Power = Fv

$$350 \times 10^3 = T \times 6.107$$

$$T = \frac{350 \times 10^3}{6.107}$$

Using F = ma:

$$T - 6 \times 10^3 = 150 \times 10^3 \times a$$

$$\frac{350 \times 10^3}{6.107} - 6 \times 10^3 = 150 \times 10^3 \times a$$

$$150a = \frac{350}{6.107} - 6$$
$$a = 0.3420...$$

The initial acceleration is  $0.342~\text{m s}^{-2}$  (3 s.f.)

$$16 \longrightarrow 0 \text{ m s}^{-2} \longrightarrow v \text{ m s}^{-2}$$

$$150 + 3v \longrightarrow T$$

Power = 
$$10 \text{ kW} = 10 000 \text{ W}$$

Power = 
$$Tv$$

$$10\ 000 = Tv$$

$$T = \frac{10000}{v}$$

When the velocity is maximum, the acceleration =  $0 \text{ m s}^{-2}$ Therefore the resultant force is 0 N. Resolving horizontally:

$$T = 150 + 3v$$
So 
$$\frac{10\ 000}{v} = 150 + 3v$$

$$10\ 000 = 150v + 3v^2$$

Rearranging:

$$3v^2 + 150v - 10000 = 0$$

Using the quadratic formula:

$$v = \frac{-150 \pm \sqrt{150^2 - 4 \times 3 \times (-10000)}}{\frac{6}{6}}$$
$$v = \frac{-150 \pm \sqrt{142500}}{6}$$

Since 
$$v > 0$$
,  $v = \frac{-150 + \sqrt{142500}}{6} = 37.91...$ 

The maximum value of v is 37.9 m s<sup>-1</sup> (3 s.f.)

17 a



$$1200 + 8v \longrightarrow 4000 \text{ kg} \longrightarrow T$$

Power = 
$$28 \text{ kW} = 28\,000 \text{ W}$$

Power = 
$$Tv$$

$$28\,000 = Tv$$

$$T = \frac{28\,000}{v}$$

Resolving horizontally and using F = ma:

$$\frac{28\,000}{v} - (1200 + 8v) = 4000a$$

When 
$$v = 10 \text{ m s}^{-1}$$
:

$$2800 - (1200 + 80) = 4000a$$

$$1520 = 4000a$$

$$50 = 4000a$$
So  $a = \frac{1520}{4000} = 0.38 \text{ m s}^{-2}$ 

**b** Using P = Fv, when the van is travelling at speed w:

$$28\ 000 = Tw$$

$$T = \frac{28\,000}{w}$$

Resistive force = 1200 + 8w

As in part **a**, resolving horizontally and using F = ma:

$$\frac{28\,000}{w} - \left(1200 + 8w\right) = 4000a$$

When 
$$v = w \text{ m s}^{-1}$$
,  $a = -0.2 \text{ m s}^{-2}$ :

$$\frac{28\,000}{w} - (1200 + 8w) = 4000 \times (-0.2)$$

$$28\,000 - 1200w - 8w^2 = -800w$$

$$8w^2 + 400w - 28000 = 0$$

$$w^2 + 50w - 3500 = 0$$

Using the quadratic formula:

$$w = \frac{-50 \pm \sqrt{50^2 - 4 \times 1 \times (-3500)}}{2} = \frac{-50 \pm \sqrt{16500}}{2}$$

Since 
$$w > 0$$
,  $w = \frac{-50 + \sqrt{16500}}{2} = 39.22...$ 

The value of w is 39.2 (3 s.f.)