

Straight line graphs 5E

1 a $y = 5x - 2, m = 5$

$$15x - 3y + 9 = 0$$

Parallel lines have the same gradient.

Rearrange the second equation to give:

$$3y = 15x + 9$$

$$y = 5x + 3, m = 5$$

The lines have the same gradients so are parallel.

b $7x + 14y - 1 = 0$

$$y = \frac{1}{2}x + 9, m = \frac{1}{2}$$

Parallel lines have the same gradient.

Rearrange the first equation to give:

$$14y = -7x + 1$$

$$y = -\frac{1}{2}x + \frac{1}{14}, m = -\frac{1}{2}$$

The lines have different gradients so are not parallel.

c $4x - 3y - 8 = 0$

$$3x - 4y - 8 = 0$$

Parallel lines have the same gradient.

Rearrange the first equation to give:

$$3y = 4x - 8$$

$$y = \frac{4}{3}x - \frac{8}{3}, m = \frac{4}{3}$$

Rearrange the second equation to give:

$$4y = 3x - 8$$

$$y = \frac{3}{4}x - 2, m = \frac{3}{4}$$

The lines have different gradients so are not parallel.

2 The gradient of r is:

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - 4}{6 - 1}$$

$$= \frac{4}{5}$$

The gradient of s is:

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{9 - (-3)}{20 - 5}$$

$$= \frac{12}{15}$$

$$= \frac{4}{5}$$

2 The gradients are equal, so the lines are parallel.

3 If $A(-6, 2)$, $B(4, 8)$, $C(6, 1)$ and $D(-9, -8)$ are coordinates of a trapezium, line AB is parallel to CD or BC is parallel to DA .

Parallel lines have the same gradient.

$$\begin{aligned} \text{The gradient of } AB &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{8 - 2}{4 - (-6)} \\ &= \frac{6}{10} \\ &= \frac{3}{5} \end{aligned}$$

$$\begin{aligned} \text{The gradient of } CD &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{-8 - 1}{-9 - 6} \\ &= \frac{-9}{-15} \\ &= \frac{3}{5} \end{aligned}$$

Gradient of AB = gradient of CD .

AB is parallel to CD , therefore $ABCD$ is a trapezium.

4 The line is parallel to $y = 5x + 8$, so $m = 5$.

The line intercepts the y -axis at $(0, 3)$, so $c = 3$.

Using $y = mx + c$, the equation of the line is $y = 5x + 3$.

5 The line is parallel to $y = -\frac{2}{5}x + 1$, so $m = -\frac{2}{5}$.

The line intercepts the y -axis at $(0, -4)$, so $c = -4$.

- 5** Using $y = mx + c$, the equation of the line is

$$y = -\frac{2}{5}x - 4.$$

Multiply each term by 5:

$$5y = -2x - 20$$

$$2x + 5y = -20$$

$$2x + 5y + 20 = 0$$

- 6** $3x + 6y + 11 = 0$

$$6y + 11 = -3x$$

$$6y = -3x - 11$$

$$y = -\frac{3}{6}x - \frac{11}{6}$$

$$y = -\frac{1}{2}x - \frac{11}{6}$$

The line is parallel to $y = -\frac{1}{2}x - \frac{11}{6}$,

so $m = -\frac{1}{2}$.

The line intercepts the y-axis at $(0, 7)$,

so $c = 7$.

Using $y = mx + c$, the equation of the line is $y = -\frac{1}{2}x + 7$.

- 7** $2x - 3y - 1 = 0$

$$2x - 1 = 3y$$

$$3y = 2x - 1$$

$$y = \frac{2}{3}x - \frac{1}{3}$$

The line is parallel to $y = \frac{2}{3}x - \frac{1}{3}$, so

$m = \frac{2}{3}$.

The line intercepts the y-axis at $(0, 0)$,

so $c = 0$.

Using $y = mx + c$:

$$y = \frac{2}{3}x + 0$$

$$y = \frac{2}{3}x$$

- 8** The gradient of a line parallel to $y = 4x + 1$ is 4.

$$y - y_1 = m(x - x_1)$$

$$y - 7 = 4(x - (-2))$$

$$y - 7 = 4(x + 2)$$

$$y - 7 = 4x + 8$$

$$y = 4x + 15$$

$$0 = 4x + 15 - y$$

$$4x - y + 15 = 0$$

The equation of the line is

$$4x - y + \frac{15}{2} = 0.$$